Mathematics

Mid-Term Exam-I

Autumn 2015

20 marks

Time: 1 Hour

[1]Find y`:

(a)
$$y = 3x^3 + 3^x - \sqrt{3}$$

(b)
$$y = \log x + \ln(x^2 + 3)$$

$$(c) y = \cos x + (\sin x)^5$$

(d)
$$y = \frac{\sin x}{x^5} + \frac{3^x}{2^x}$$

[2] Find the extrema of each function : $f(x) = \frac{x}{3} + \frac{3}{x}$

[3] Find the integrals:

(a)
$$\int (2^x - \sin x) \, dx$$

(b)
$$\int (x^3 + \cos 3x) \, dx$$

(a)
$$\int (2^x - \sin x) dx$$
 (b) $\int (x^3 + \cos 3x) dx$ (c) $\int (\frac{1}{x} - \frac{3}{x+5}) dx$ (d) $\int (x^2 - 2x)^2 dx$ (e) $\int \cos x \cdot (\sin x)^8 dx$ (f) $\int x \cos x dx$

(d)
$$\int (x^2 - 2x)^2 dx$$

(e)
$$\int \cos x \cdot (\sin x)^8 dx$$

(f)
$$\int x \cos x \, dx$$

[4]If y is the quantity of a drug decreases according to the equation : $\frac{dy}{dt} = -y$.

Find y as function of the time t where the initial quantity is 10 units.

Also, find the value of y after 3 hours.